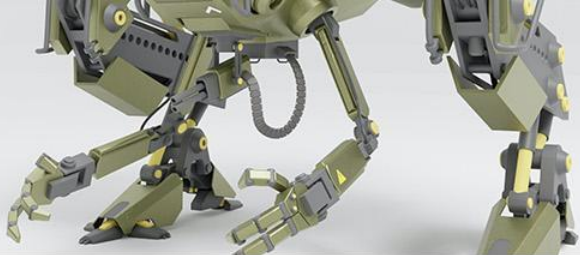


## UNIT III

# Adversarial Search and Games



# Contents



## Unit III

## Adversarial Search and Games

07 Hours

Game Theory, Optimal Decisions in Games, Heuristic Alpha–Beta Tree Search, Monte Carlo Tree Search, Stochastic Games, Partially Observable Games, Limitations of Game Search Algorithms, Constraint Satisfaction Problems (CSP), Constraint Propagation: Inference in CSPs, Backtracking Search for CSPs.

### #Exemplar/Case Studies

Machine Learning At Google: The Amazing Use Case Of Becoming A Fully Sustainable Business

### \*Mapping of Course Outcomes for Unit III

CO3, CO4

# Game Theory



## **Adversarial Search:**

Adversarial search is a search, where we examine the problem which arises when we try to plan ahead of the world and other agents are planning against us.

# Game Theory



## Types of Games in AI:

	Deterministic	Chance Moves
Perfect information	Chess, Checkers, go, Othello	Backgammon, monopoly
Imperfect information	Battleships, blind, tic-tac-toe	Bridge, poker, scrabble, nuclear war

## Game Theory



**Perfect information:** A game with the perfect information is that in which agents can look into the complete board. Agents have all the information about the game, and they can see each other moves also. Examples are Chess, Checkers, etc.

**Imperfect information:** If in a game agents do not have all information about the game and not aware with what's going on, such type of games are called the game with imperfect information, such as tic-tac-toe, Battleship, blind, Bridge, etc.

# Game Theory



**Deterministic games:** Deterministic games are those games which follow a strict pattern and set of rules for the games, and there is no randomness associated with them.

Examples are chess, Checkers, Go, tic-tac-toe, etc.

**Non-deterministic games:** Non-deterministic are those games which have various unpredictable events and has a factor of chance or luck. This factor of chance or luck is introduced by either dice or cards. These are random, and each action response is not fixed. Such games are also called as stochastic games.

Example: Backgammon, Monopoly, Poker, etc.





## Zero-Sum Game:

- Zero-sum games are adversarial search which involves pure competition.
- In Zero-sum game each agent's gain or loss of utility is exactly balanced by the losses or gains of utility of another agent.
- One player of the game try to maximize one single value, while other player tries to minimize it.
- Each move by one player in the game is called as ply.
- Chess and tic-tac-toe are examples of a Zero-sum game.

# Optimal Decisions in Games



## Minimax Algorithm

- Mini-max algorithm is a recursive or backtracking algorithm which is used in decision-making and game theory.
- It provides an optimal move for the player assuming that opponent is also playing optimally.
- Mini-Max algorithm uses recursion to search through the game-tree.
- Min-Max algorithm is mostly used for game playing in AI. Such as Chess, Checkers, tic-tac-toe, go, and various two-players game. This Algorithm computes the minimax decision for the current state.



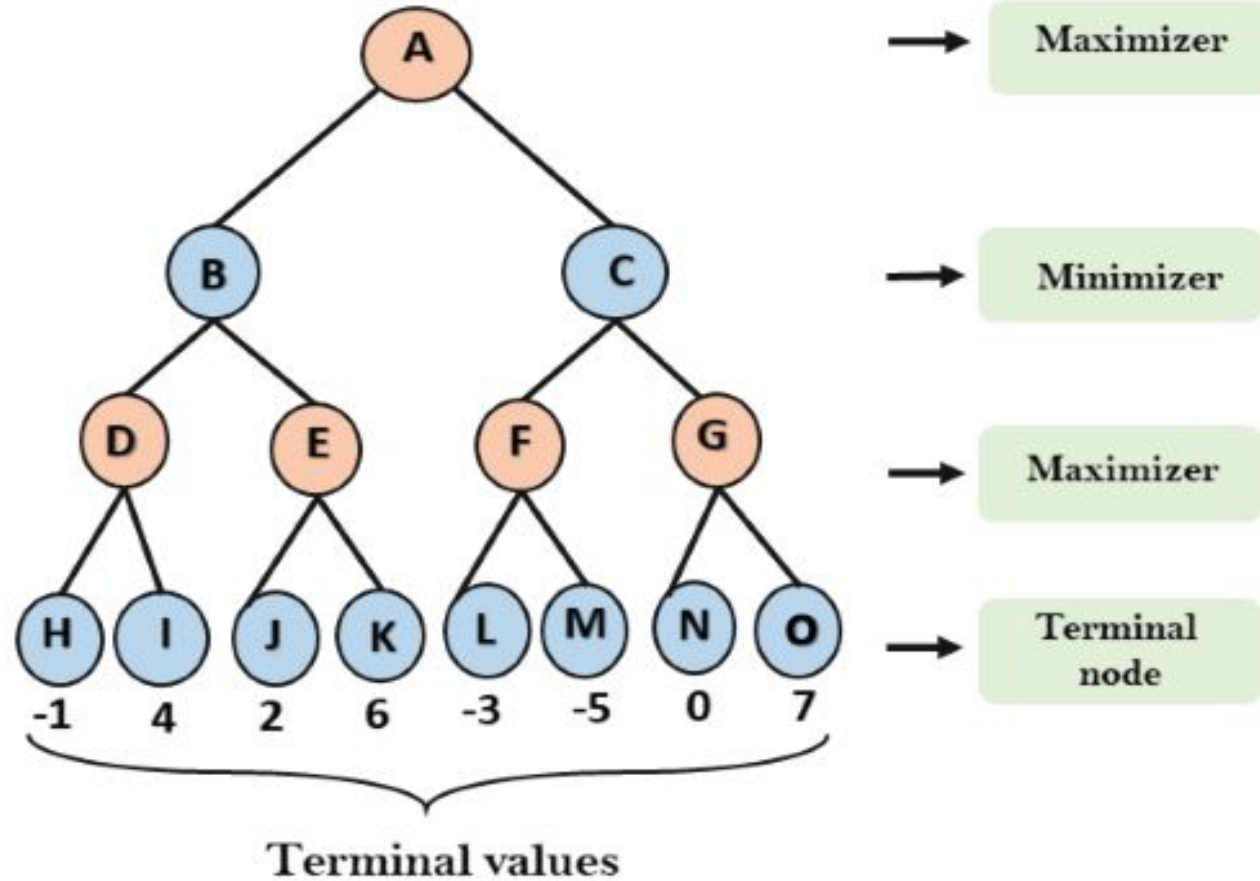
## Optimal Decisions in Games



- ▮ In this algorithm two players play the game, one is called MAX and other is called MIN.
- ▮ Both the players fight it as the opponent player gets the minimum benefit while they get the maximum benefit.
- ▮ Both Players of the game are opponent of each other, where MAX will select the maximized value and MIN will select the minimized value.
- ▮ The minimax algorithm performs a depth-first search algorithm for the exploration of the complete game tree.
- ▮ The minimax algorithm proceeds all the way down to the terminal node of the tree, then backtrack the tree as the recursion.

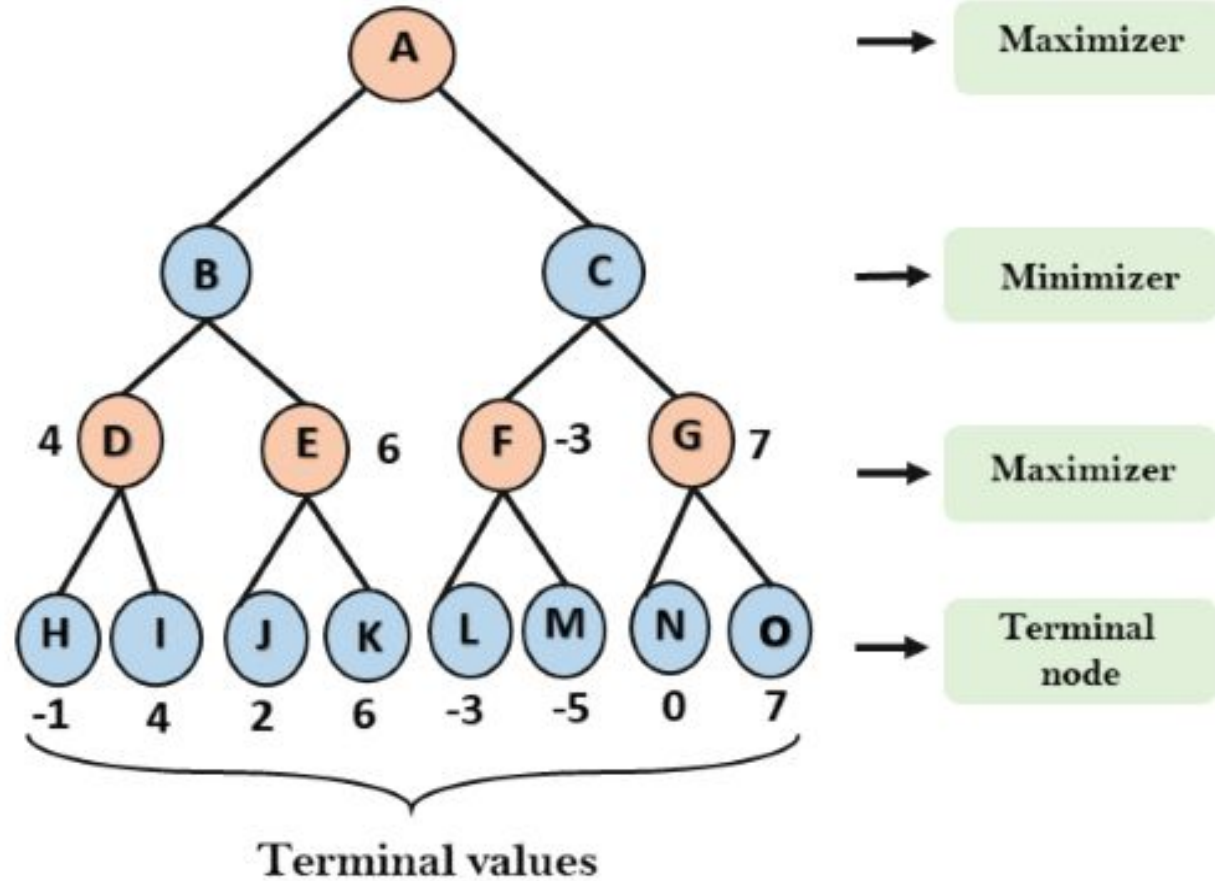
# Optimal Decisions in Games

Working of Min-Max  
Algorithm:



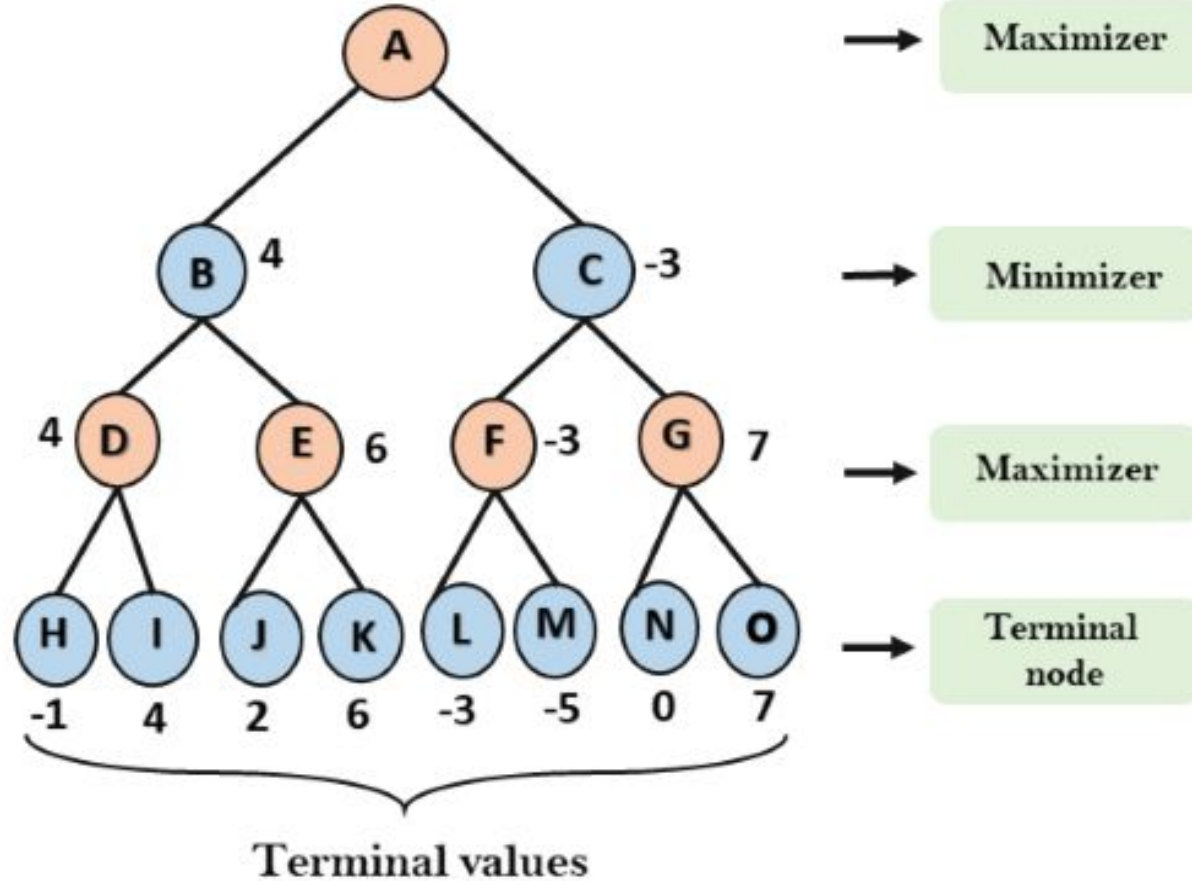
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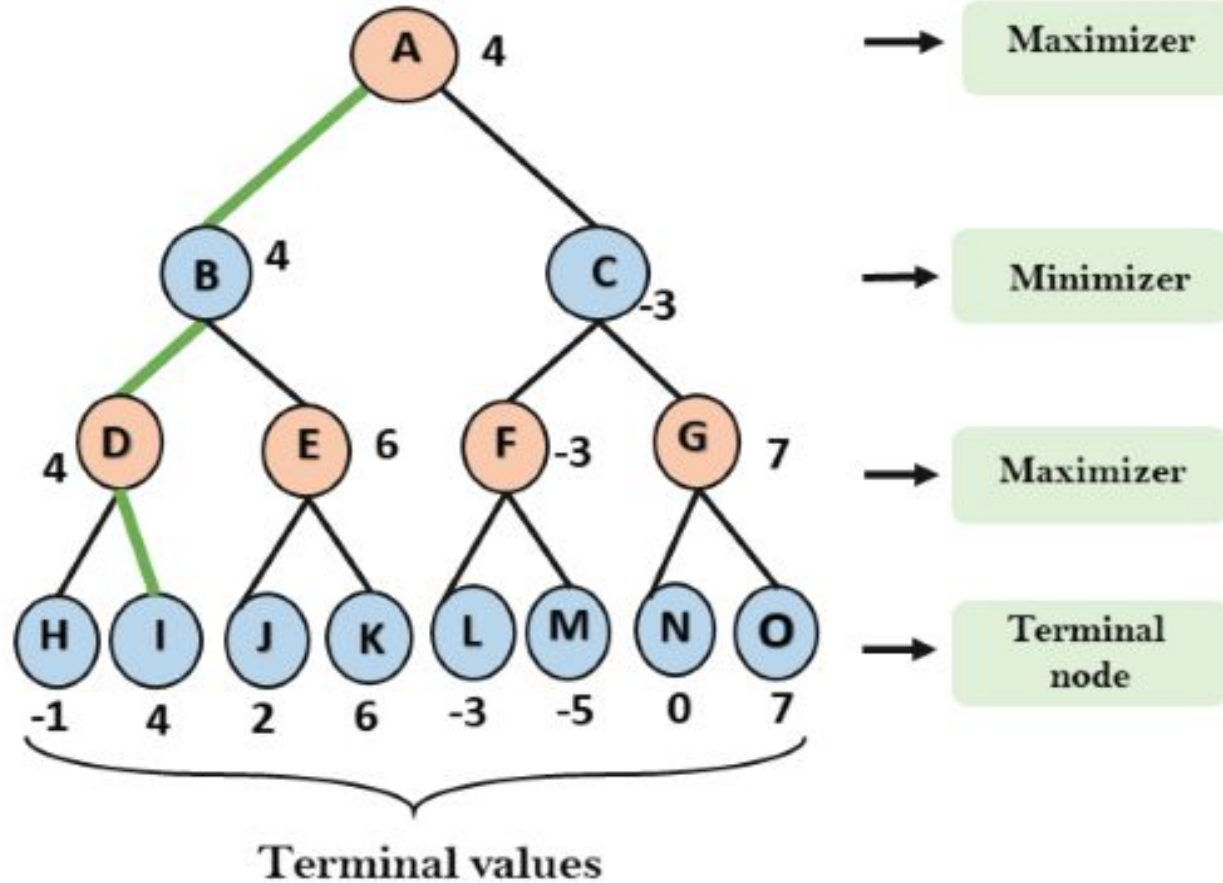
# Optimal Decisions in Games

Working of Min-Max  
Algorithm:



# Optimal Decisions in Games

Working of Min-Max  
Algorithm:



# Optimal Decisions in Games



Properties of Mini-Max algorithm:

- **Complete-** Min-Max algorithm is Complete. It will definitely find a solution (if exist), in the finite search tree.
- **Optimal-** Min-Max algorithm is optimal if both opponents are playing optimally.
- **Time complexity-** As it performs DFS for the game-tree, so the time complexity of Min-Max algorithm is  $O(b^d)$ , where  $b$  is branching factor of the game-tree, and  $d$  is the maximum depth of the tree.
- **Space Complexity-** Space complexity of Mini-max algorithm is also similar to DFS which is  $O(bd)$ .

# Optimal Decisions in Games



Limitation of the minimax Algorithm:

- The main drawback of the minimax algorithm is that it gets really slow for complex games such as Chess, go, etc.
- This type of games has a huge branching factor, and the player has lots of choices to decide. This limitation of the minimax algorithm can be improved from alpha-beta pruning